

# DOGBALL

*A summary of the main aspects*

This currently-brief summary assumes that you attended a workshop at which Dogball appeared. Either a 3-hour workshop, or a 50-minute workshop (in which everything happened very quickly). ☺

It may not follow, exactly how our workshop unfolded – it seemed to be a little different each time, depending on what you asked and said.

## **Introduction**

Balls have both flight and bounce characteristics.

Vary some aspect of a ball and it will fly differently and bounce differently.

Who would have thought knowing something about this would matter. Have a read of

<https://en.wikipedia.org/wiki/Deflategate>

So how might be study the bounce characteristics of a ball. What ball might be a good ball, educationally speaking. It turns out that Dogball is the gun!



## **The problem**

Describe how Dogball bounces.

## **The beginning step**

Let Dogball fall freely and bounce until he bounces no more. Use a motion sensor to record the distance ( $d$ ) between the sensor and the top of dogball.

With the system we used,  $d$  was recorded every 0.02 of a second, for a little over



## **Your-task 1**

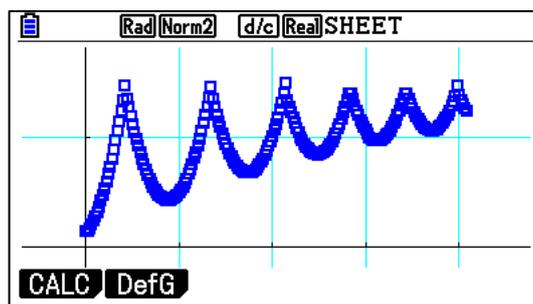
Without seeing the data, draw what you think the graph of  $d$  vs  $t$  will look like.



Do you recall what you drew?

### The next step

Graph the data.



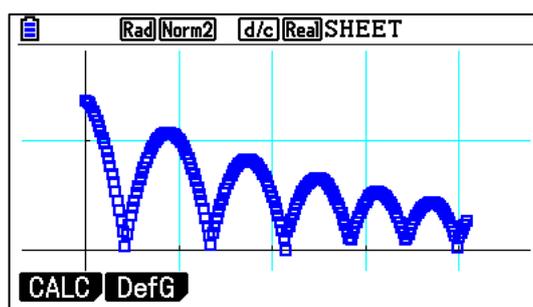
### Your-task 2

Make a list of things that come to mind as you look at the graph of the data.

- Is there something you want to do?
- Was there a realisation you came too – oh, yes, right!
- Did it make you wonder ...

### The next step

“Flip” the data.  $d$  is now a different quantity.



### Your-task 3

When did the 10<sup>th</sup> peak occur and how high was Dogball at that time?

You might recall this being a less than straight forward task.

Use trace to pick out the time and distance of Dogball’s top of flight positions.

Peak number $n$	1	2	3	4	5	6
$t$	0	0.88	1.72	2.48	3.12	3.72
$d$	1.36	1.07	0.83	0.66	0.53	0.44

Calculate some ratios or determine some models using regression.

$$d = 1.39(0.737)^t \quad d = 1.68(0.796)^n$$

Over to you to recall the rest. How close was your prediction?

Recall we talked about [https://en.wikipedia.org/wiki/Coefficient\\_of\\_restitution](https://en.wikipedia.org/wiki/Coefficient_of_restitution)

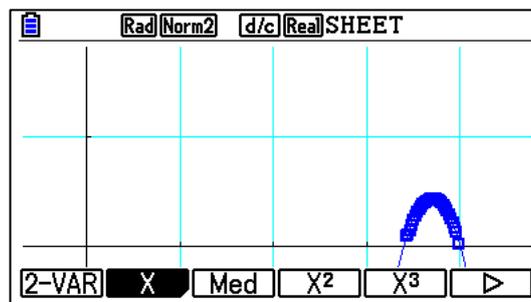
As such, “ $b$ ”, is in fact not a constant.

#### Your-task 4

What Dogball's position at  $t = 6.7$  seconds? (Perhaps not at a peak!)

Recall we isolated sections of the motion and developed a piece-wise model for  $d$  in terms of  $t$ .

Below you can see the last section.



The model we developed is given below:

$$d = -5.18t^2 - 0.95t + 1.37 \text{ for } 0 \leq t < 0.42$$

$$d = -4.8t^2 + 8.49t - 2.66 \text{ for } 0.42 \leq t < 1.34$$

$$d = -4.87t^2 + 16.93t - 13.85 \text{ for } 1.34 \leq t < 2.14$$

$$d = -4.85t^2 + 24.11t - 29.3 \text{ for } 2.14 \leq t \leq 2.84$$

$$d = -5.17t^2 + 32.36t - 50 \text{ for } 2.84 \leq t \leq 3.42$$

$$d = -4.79t^2 + 35.5t - 65.2 \text{ for } 3.42 \leq t \leq 3.98$$

We then stood back and observed the coefficients and ...

We then considered writing this set as 'one', replacing the coefficients with functions.

And that was about it.